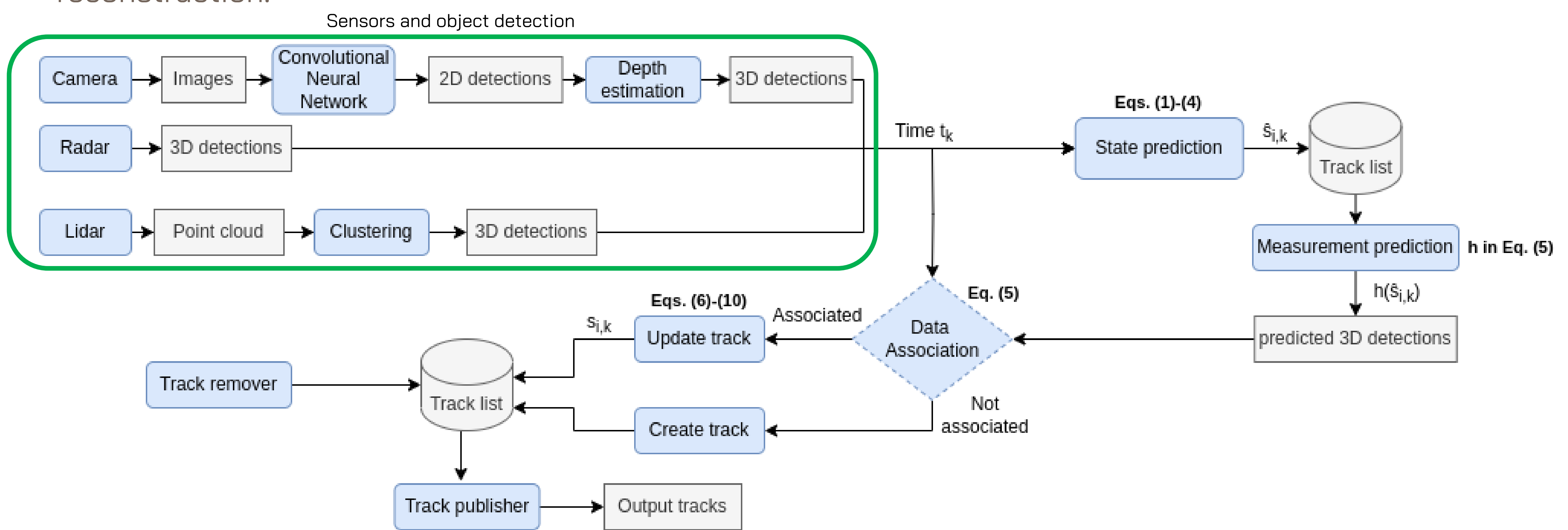


# Robust Multimodal and Multi-Object Tracking for Autonomous Driving Applications

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- Sensor-agnostic multimodal fusion framework for multiple object tracking that can seamlessly integrate information coming from different object detectors, sensors, and vehicle-to-everything messages, either from other road users or from the infrastructure.
- All the information received is converted to a standardized set of detections that are then combined using a Kalman Filter with a constant velocity model.
- To ensure robustness, we propose methods to handle errors in classification and incorrect bounding box reconstruction.



The  $i$ -th tracklet has the state  $\mathbf{s}_{k,i} = [r_x, r_y, v_x, v_y]^T \in \mathbb{R}^4$  and its covariance  $\mathbf{P}_{k,i} \in \mathbb{R}^{4 \times 4}$ .

### State prediction

$$\hat{\mathbf{s}}_{k,i} = \mathbf{F}(\Delta t) \mathbf{s}_{k-1,i} \quad (1)$$

$$\mathbf{F}(\Delta t) = \begin{bmatrix} \mathbf{I}_2 & \Delta t \mathbf{I}_2 \\ \mathbf{0} & \mathbf{I}_2 \end{bmatrix} \quad (2)$$

$$\hat{\mathbf{P}}_{k,i} = \mathbf{F}(\Delta t) \mathbf{P}_{k-1,i} \mathbf{F}(\Delta t)^T + \mathbf{Q}(\Delta t) \in \mathbb{R}^{4 \times 4} \quad (3)$$

$$\mathbf{Q}(\Delta t) = \begin{bmatrix} \mathbf{I}_2 & \mathbf{0} \\ \mathbf{0} & b \Delta t \mathbf{I}_2 \end{bmatrix} \quad (4)$$

### Measurement prediction

From state to measurement space:  $h: \mathbb{R}^4 \rightarrow \mathbb{R}^m$

### Data association

Mahalanobis distance  $d(\hat{\mathbf{s}}_{k,i}, \mathbf{d}_{k,j}): \mathbb{R}^4 \times \mathbb{R}^m \rightarrow \mathbb{R}$  defined by:

$$d = \sqrt{(\mathbf{d}_{k,j} - h(\hat{\mathbf{s}}_{k,i}))^T \Sigma_{k,i,j}^{-1} (\mathbf{d}_{k,j} - h(\hat{\mathbf{s}}_{k,i}))} \quad (5)$$

### Update track

Mean and covariance of the innovation:  $\mathbf{y}_{k,i} = \mathbf{d}_{k,j} - h(\hat{\mathbf{s}}_{k,i}) \in \mathbb{R}^m \quad (6)$

$$\Sigma_{k,i,j} = \mathbf{H} \hat{\mathbf{P}}_{k,i} \mathbf{H}^T + \mathbf{R}_{k,j} \in \mathbb{R}^{m \times m} \quad (7)$$

Where:

$\mathbf{H} \in \mathbb{R}^{m \times 4}$  the Jacobian of  $h$

$\mathbf{R}_{k,j} \in \mathbb{R}^{m \times m}$  the covariance of the detection

Detection used to update the associated tracklet following:

$$\mathbf{K}_{k,i} = \hat{\mathbf{P}}_{k,i} \mathbf{H}^T \Sigma_{k,i,j}^{-1} \in \mathbb{R}^{4 \times m} \quad (8)$$

$$\mathbf{s}_{k,i} = \hat{\mathbf{s}}_{k,i} + \mathbf{K}_{k,i} \mathbf{y}_{k,i} \in \mathbb{R}^4 \quad (9)$$

$$\mathbf{P}_{k,i} = (\mathbf{I} - \mathbf{K}_{k,i} \mathbf{H}) \hat{\mathbf{P}}_{k,i} \in \mathbb{R}^{4 \times 4} \quad (10)$$

